

Dynamics of Spiral Structure



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Master's Seminar Course

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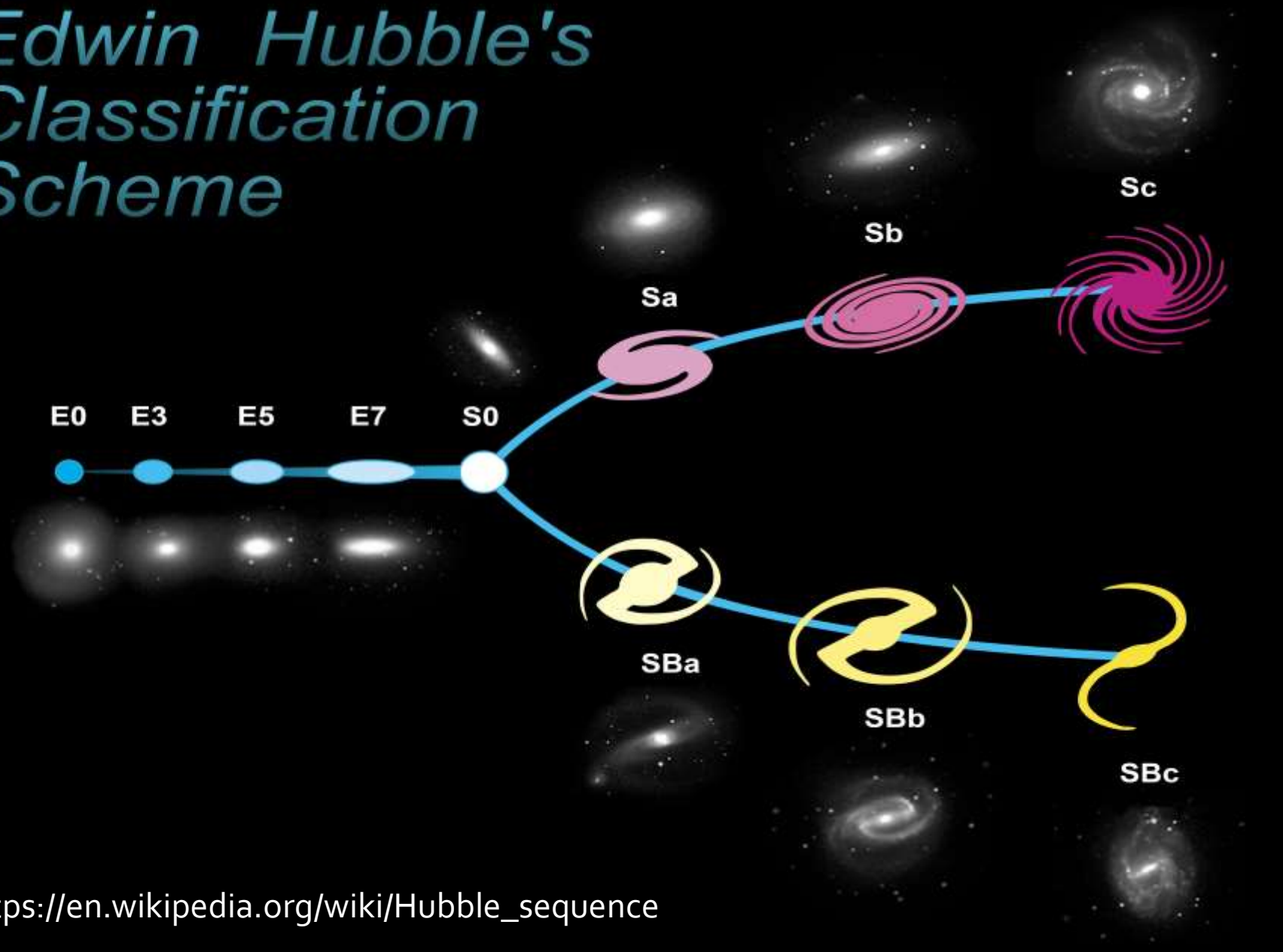
UNIVERSITÄT
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Context:

- 0. Introduction
- 1. Material Arms vs Kinetic Density Waves
- 2. Dispersion Relation
 - 2.1 LS and LSK Dispersion Relations
 - 2.2 Stability Criterion
 - 2.3 Wave Propagation
- 3. Swing Amplification
- 4. Bar-Driven Spirals
- 5. Tidal-driven Spirals
- 6. Summary

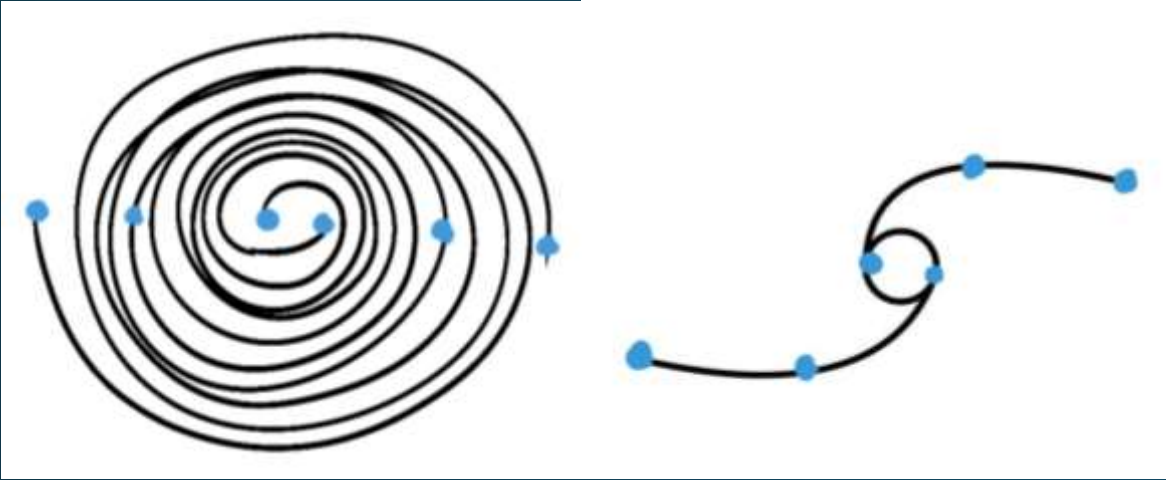
0. Introduction

Edwin Hubble's Classification Scheme



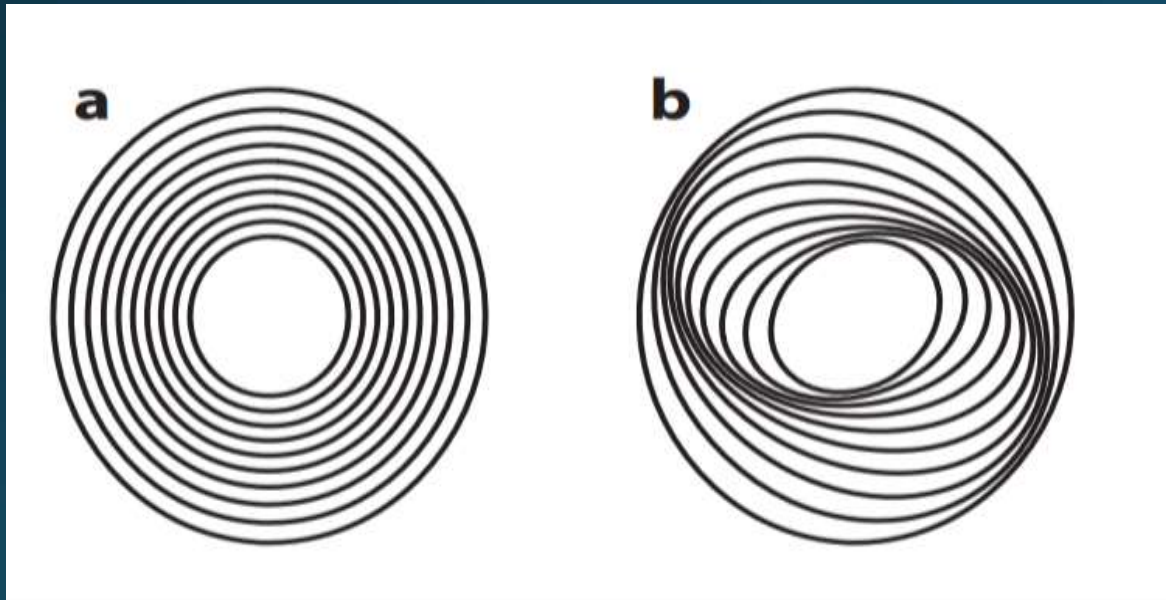
https://en.wikipedia.org/wiki/Hubble_sequence

1. Material Arms or Kinetic Density Waves



Material Arms

$$\Omega_p = \text{const.}$$



Kinetic Density Waves

$$\Omega_p = \Omega - \frac{\kappa}{2}$$

Not constant $\rightarrow$ open orbits

Winds slower

2.1- LS & LSK Dispersion Relation

- Lin-Shu (LS) Dispersion Relation (fluid)

$$(\omega - m\Omega)^2 = \underbrace{\kappa^2}_{\text{Rotation Effect}} + \underbrace{c_s^2 k^2}_{\text{Pressure}} - \underbrace{2\pi G |k| \Sigma_0}_{\text{Self-Gravity}}$$

- Lin-Shu-Kalnajs (LSK) Dispersion Relation (disc of stars)

$$(\omega - m\Omega)^2 = \kappa^2 - 2\pi G |k| \Sigma_0 F$$

Reduction factor:
Weakening of self gravity by
random motion
 $F \leq 1$

2.2 Stability Criterion

$$(\omega - m\Omega)^2 = \kappa^2 + c_s^2 k^2 - 2\pi G |k| \Sigma_0$$

$$k_{\pm} = \frac{\pi G \Sigma_0}{\kappa c_s^2} \pm \sqrt{\frac{\pi^2 G^2 \Sigma_0^2}{c_s^4} - \frac{\kappa^2}{c_s^2}} \quad \xrightarrow{\text{Toomre Parameter}} \quad Q = \frac{\kappa c_s}{\pi G \Sigma_0} \quad \begin{array}{l} \xrightarrow{\quad} Q > 1: \text{stable} \\ \xrightarrow{\quad} Q < 1: \text{unstable} \end{array}$$

$$(\omega - m\Omega)^2 = \kappa^2 - 2\pi G |k| \Sigma_0 F$$

$$\xrightarrow{\quad} Q = \frac{\kappa \sigma_R}{3.358 G \Sigma_0}$$

$$\begin{array}{l} \pi \rightarrow 3.358 \\ c_s \rightarrow \sigma_R \end{array}$$

$$\text{Cold disk: } c_s = 0 \rightarrow (\omega - m\Omega)^2 = 0 \rightarrow \text{stable if: } \lambda < \lambda_{crit} = \frac{2\pi}{k_{crit}} = \frac{4\pi^2 G \Sigma_0}{\kappa^2}$$

2.3 Wave Propagation

$$v_g = \frac{\partial \omega}{\partial k} = \pm \frac{c_s^2 |k| - \pi G \Sigma_0}{\omega - m\Omega}$$

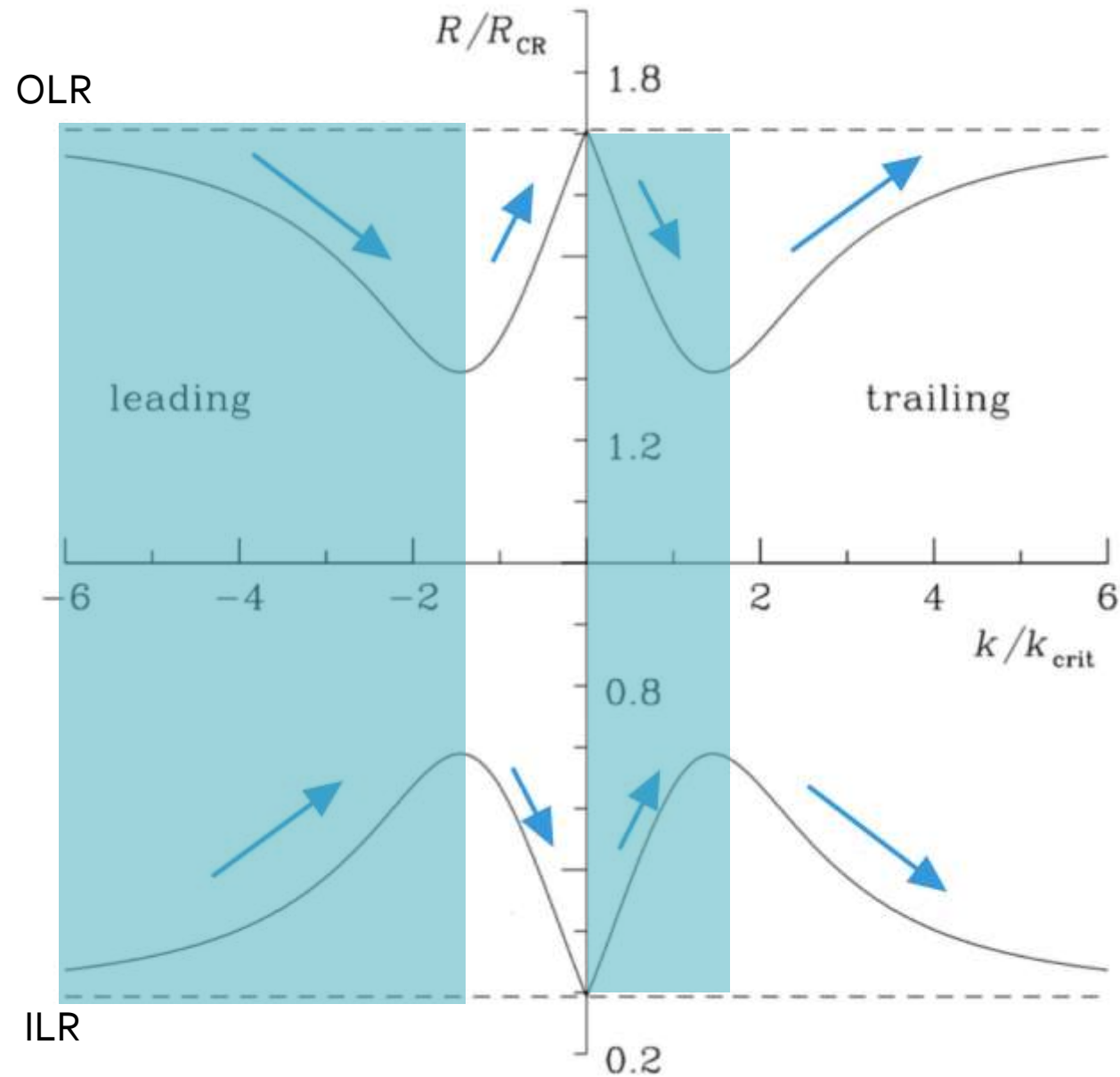
Trailing: Positive
Leading: Negative

Short waves: Positive
Long waves: Negative

$R > R_{CR}$: Positive
 $R < R_{CR}$: Negative

Short trailing And Long leading propagates away from the CR
Short Leading And Long Trailing propagates Toward the CR

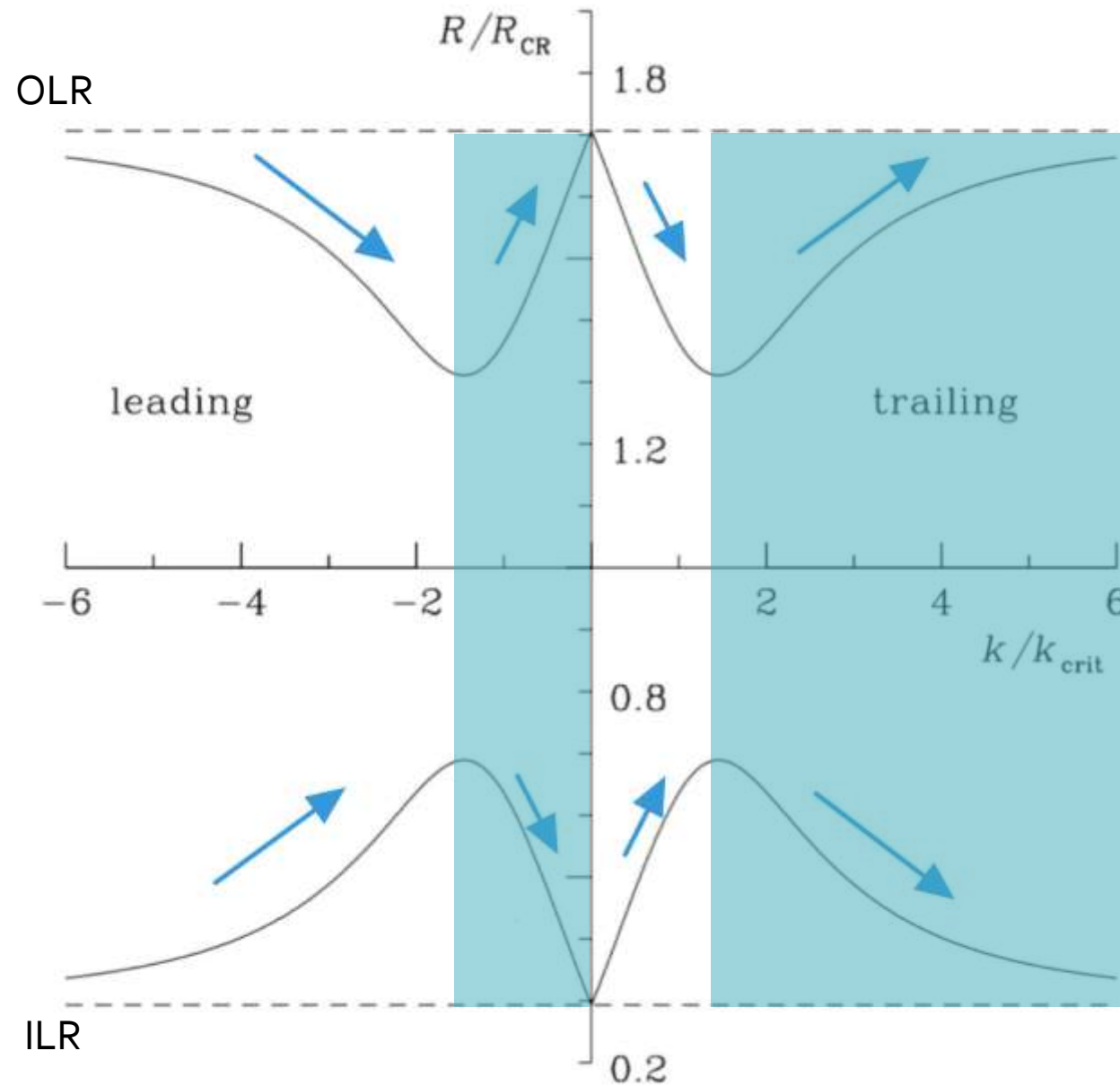
2.3 Wave Propagation



Short Leading
and
Long Trailing
propagates
Toward
the CR

Binney & Tremaine
(2008)

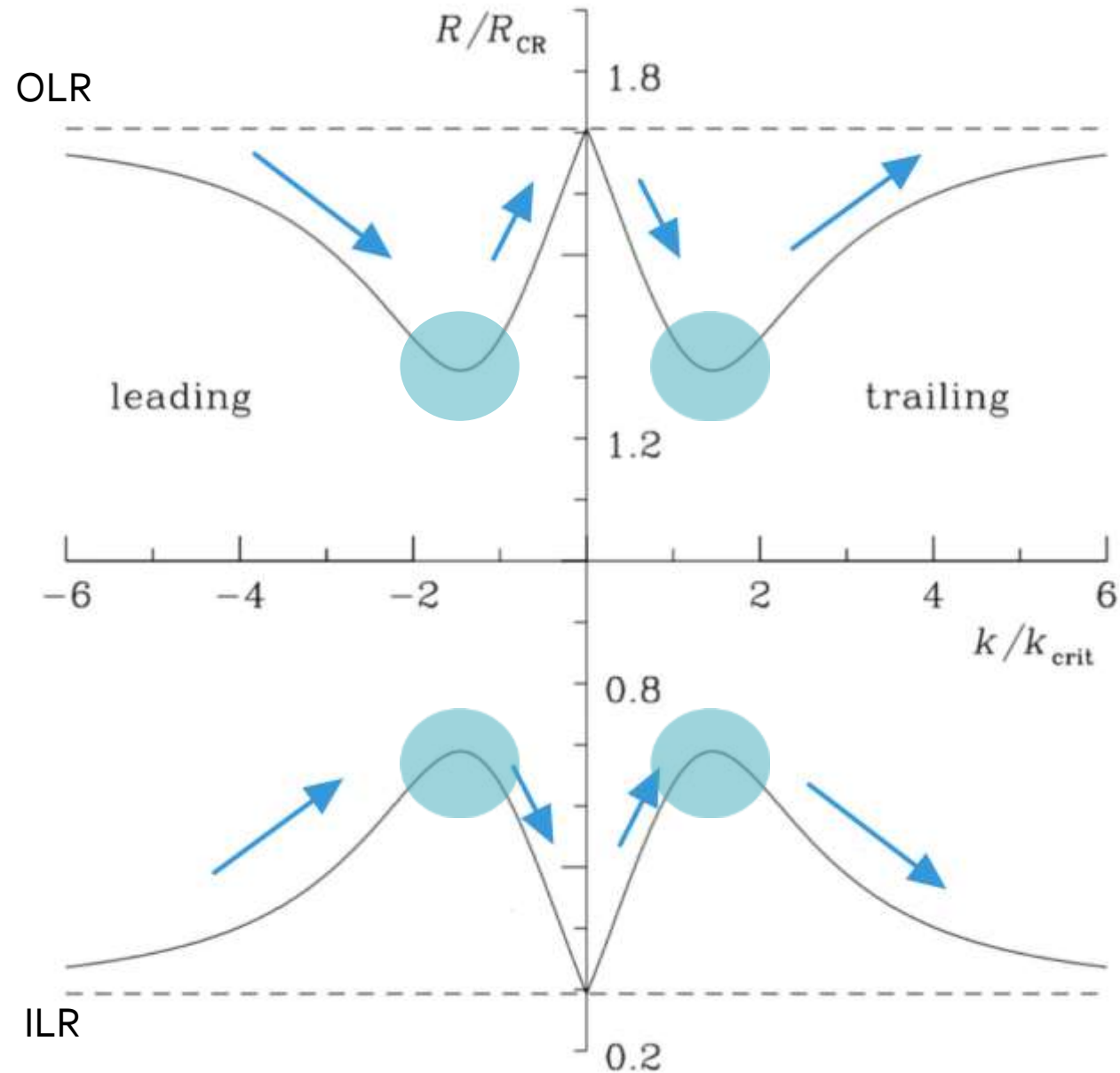
2.3 Wave Propagation



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2.3 Wave Propagation

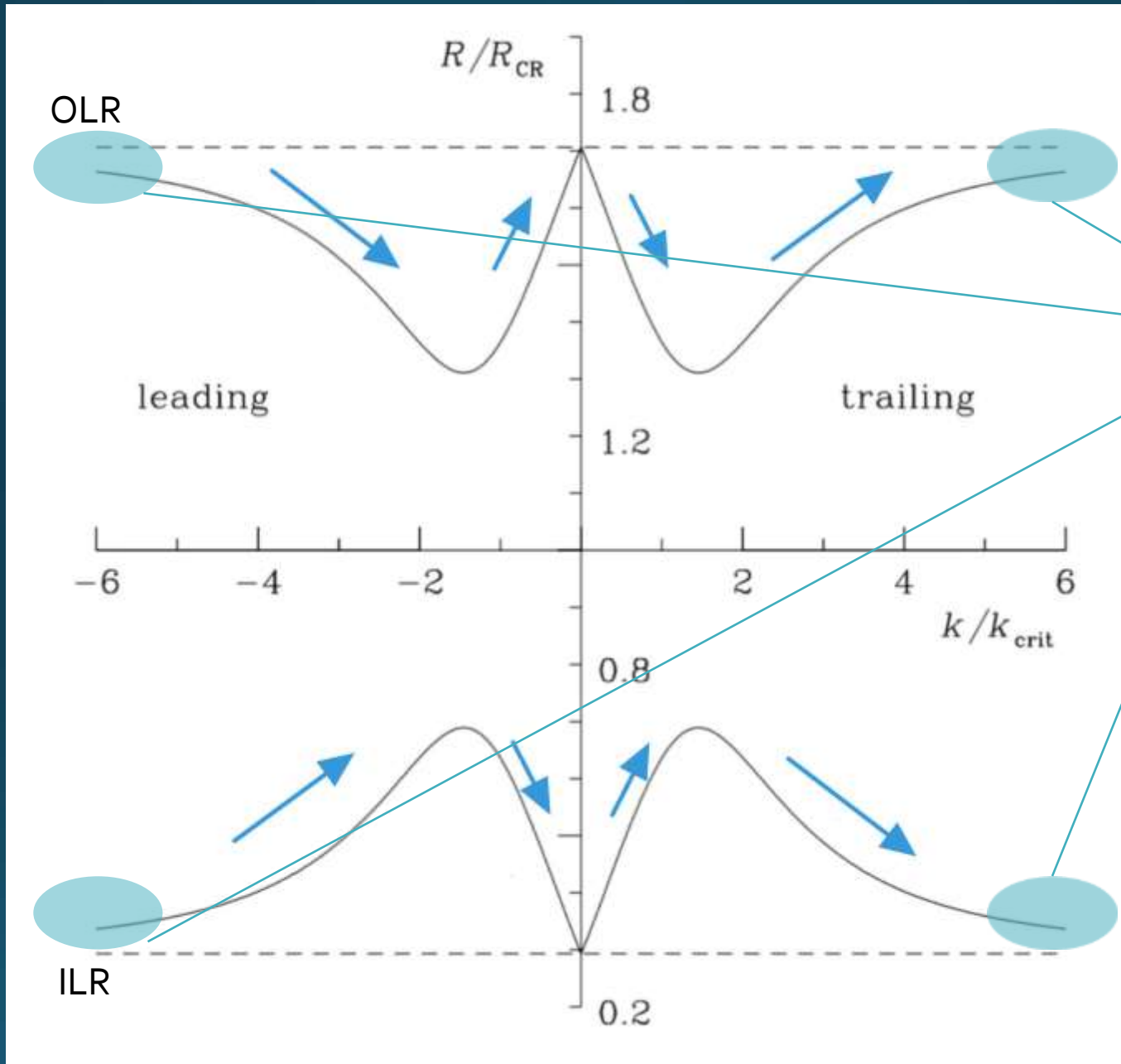


Forbidden Regions

No real solutions

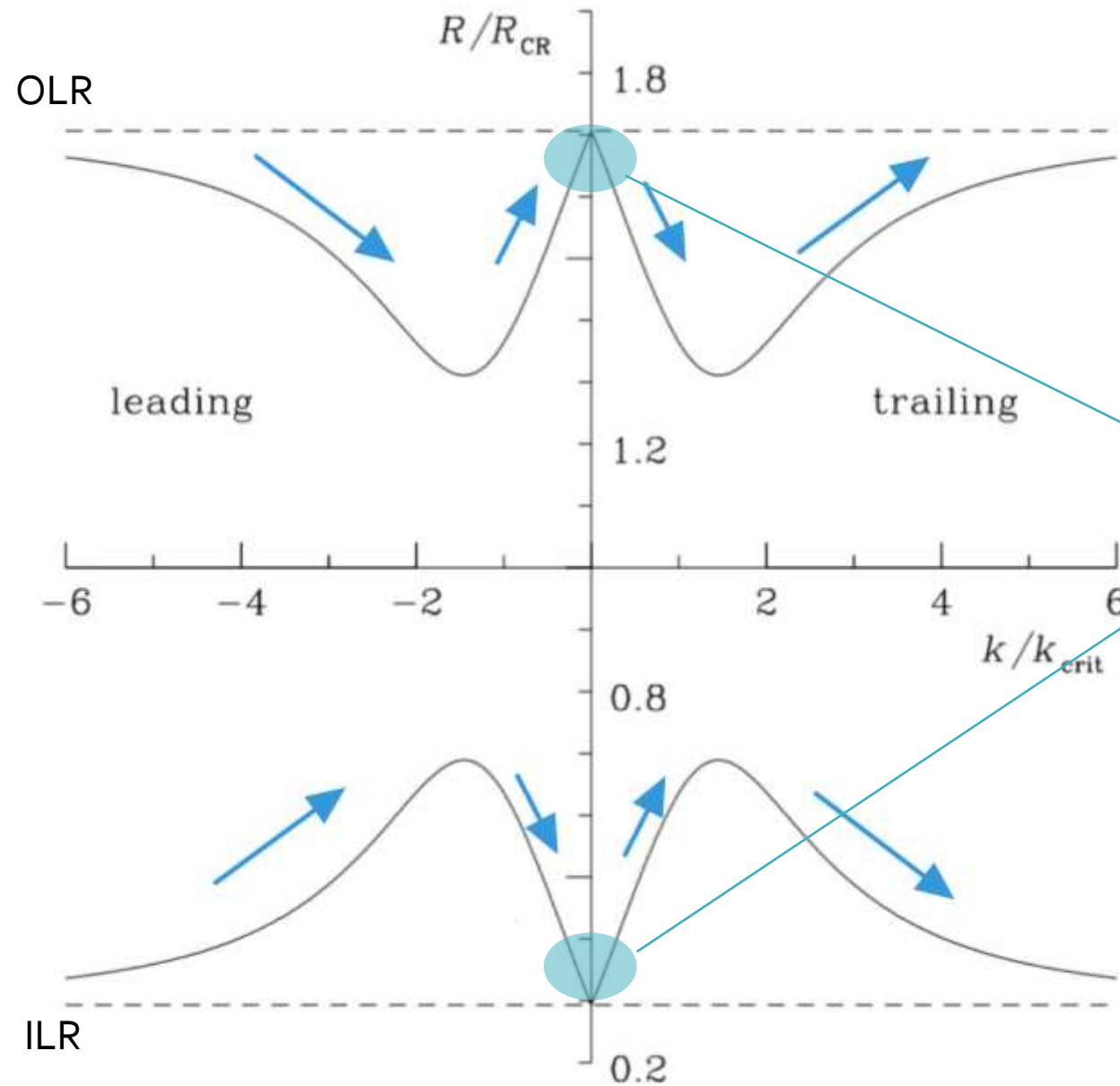
Binney & Tremaine
(2008)

2.3 Wave Propagation



short waves
absorbed due
to Landau
damping

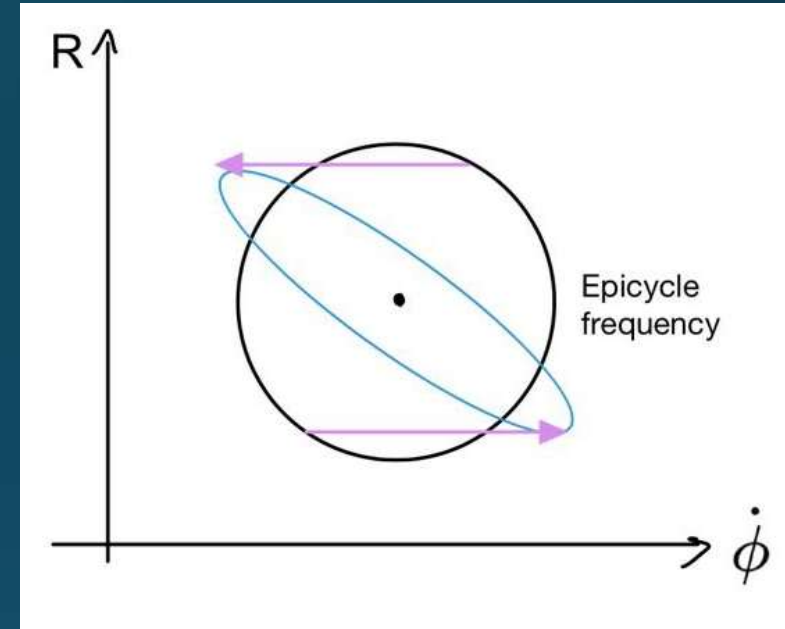
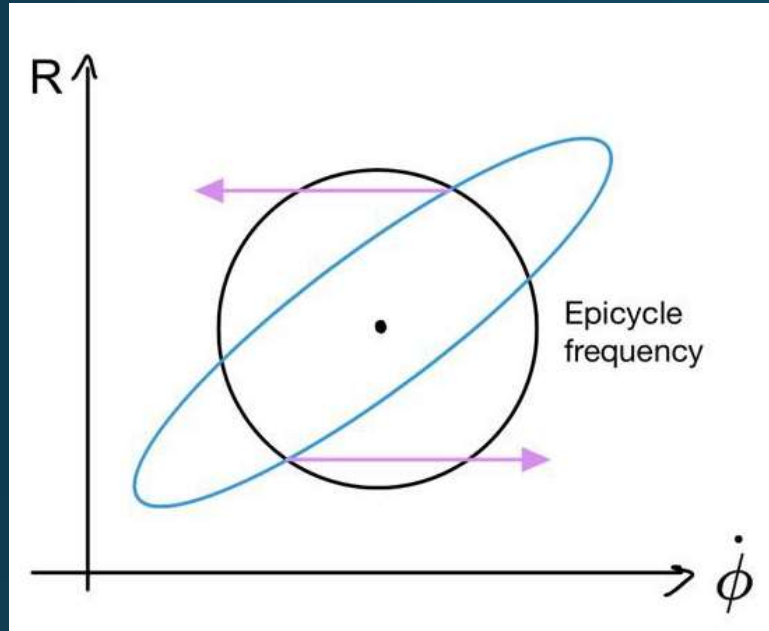
2.3 Wave Propagation



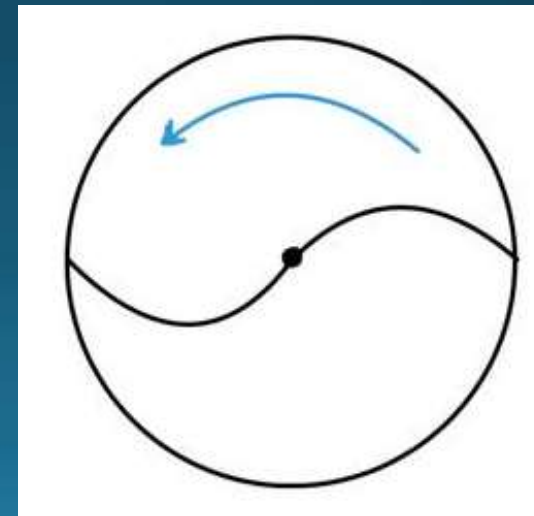
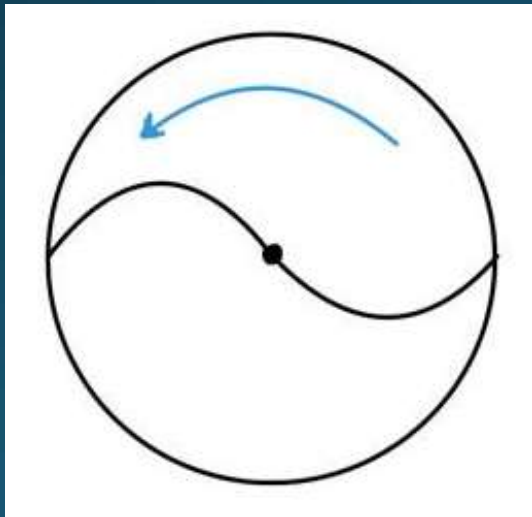
long waves
are reflected
at Lindblad
resonances

Binney & Tremaine
(2008)

3. “Swing” Amplification



LEADING



TRAILING

3. Swing “Amplification”

Normal displacement of stars


$$\ddot{\xi} + S(\gamma)\xi = 0$$

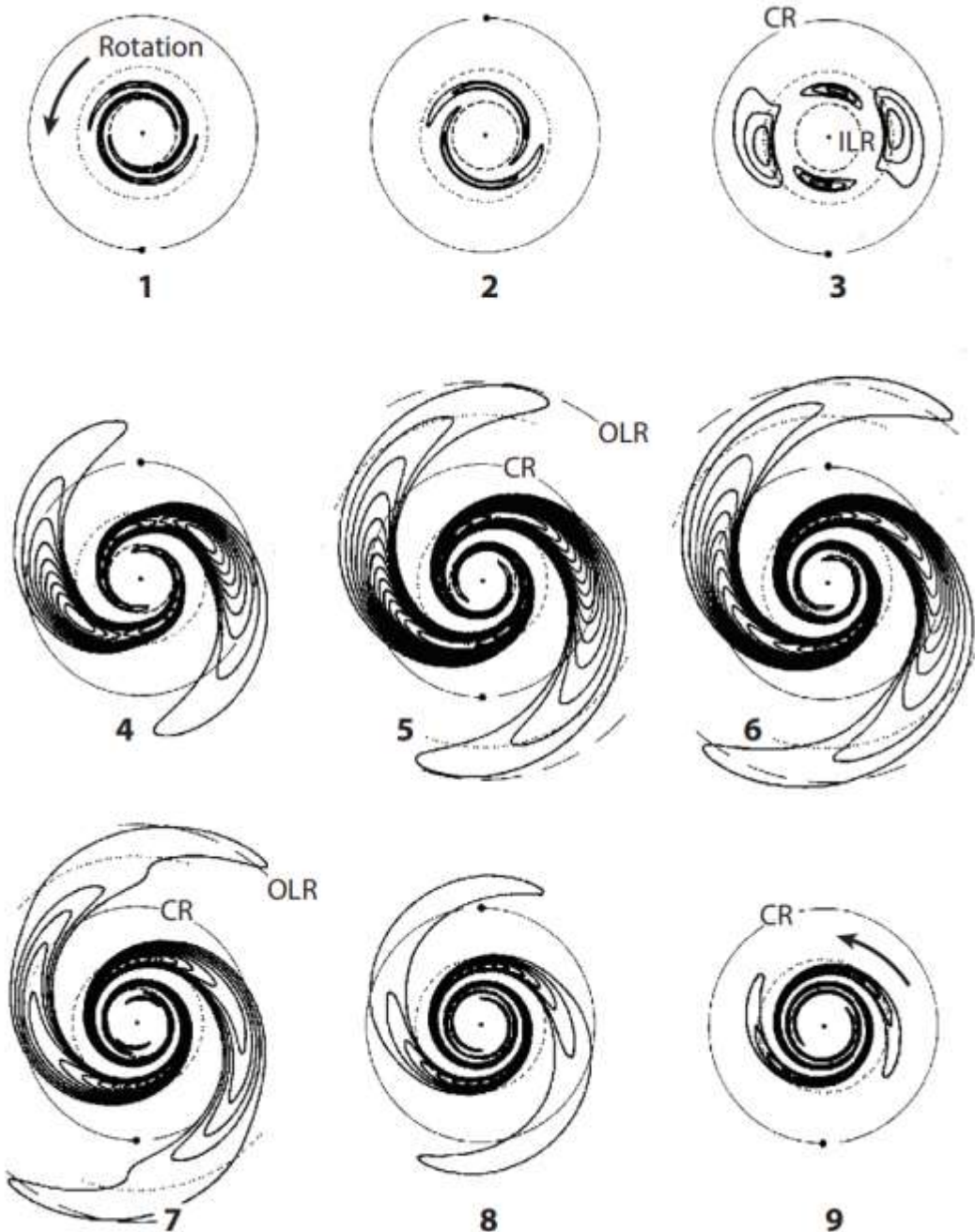
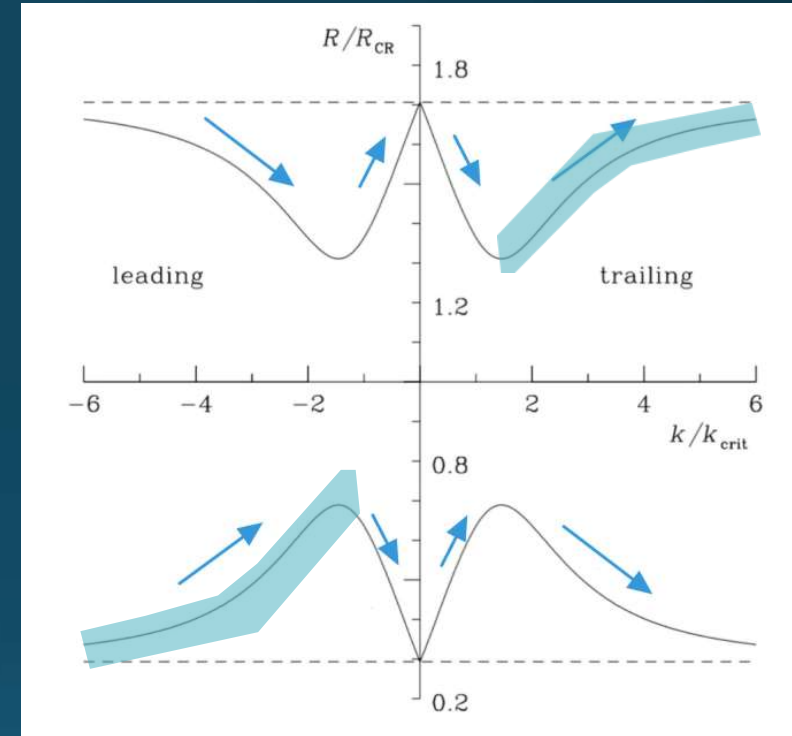
$$S(\gamma) = \left(1 - \frac{2\Gamma}{2 - \Gamma} \cos^2 \gamma + \frac{3}{2} \frac{\Gamma^2}{2 - \Gamma} \cos^4 \gamma - \frac{F}{X} \sec \gamma \right) \kappa^2$$

$$\text{effectiveness: } X = \frac{k_{crit} R}{m} \rightarrow \text{efficient } 1 \leq X \leq 2.5 \rightarrow X \approx 2 \rightarrow m = \frac{\kappa^2 R}{4\pi G \Sigma_0}$$

$$\text{shear rate: } \Gamma = -\frac{d \ln \Omega}{d \ln R} \rightarrow \Gamma = 0 \rightarrow \text{rigid body} \rightarrow S(\gamma) > 0 \rightarrow \text{spiral arms don't amplify}$$

3. Swing Amplification

- Leading wave packet with $m=2$
- Initially leading (1)
- Unwind (2)
- Open pattern (3)
- Passing CR (4)
- Trailing pattern (4)
- Amplifies (4-6)
- Winds (7-9)



- Swing amplification: short leading to short trailing
- Self-gravity increases density contrast
- Transient and keeps recurring over time

4. Bar-Driven Spirals

NGC1300

SDSS (SIMBAD)



- ☐ 2 armed barred spiral galaxies
- ☐ Same pattern speed in the spirals and the bar
- ☐ Long-lived pattern



NGC2336

SDSS (SIMBAD)

2 armed

M83

2MASS (SIMBAD)

2 armed



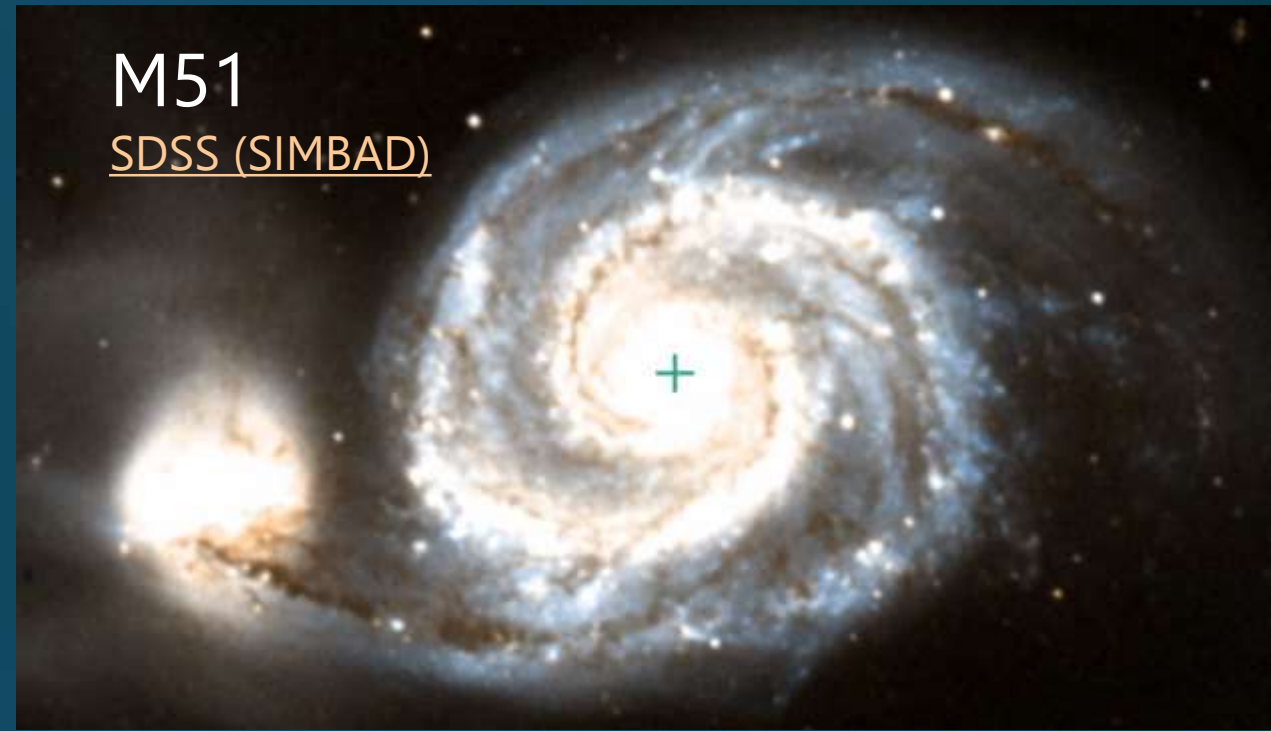
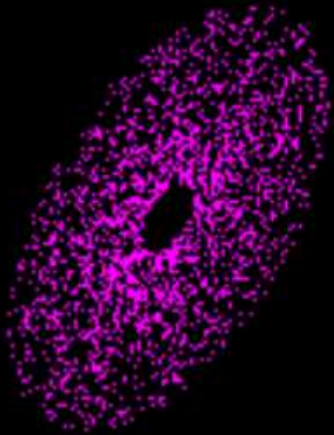
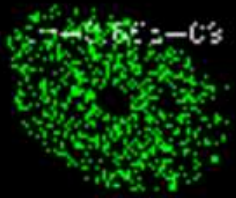
NGC1365

SDSS (SIMBAD)

same pattern speed

5. Tidal-Driven Spirals

- ❑ Close passage triggering spirals
- ❑ Two-armed grand-design pattern



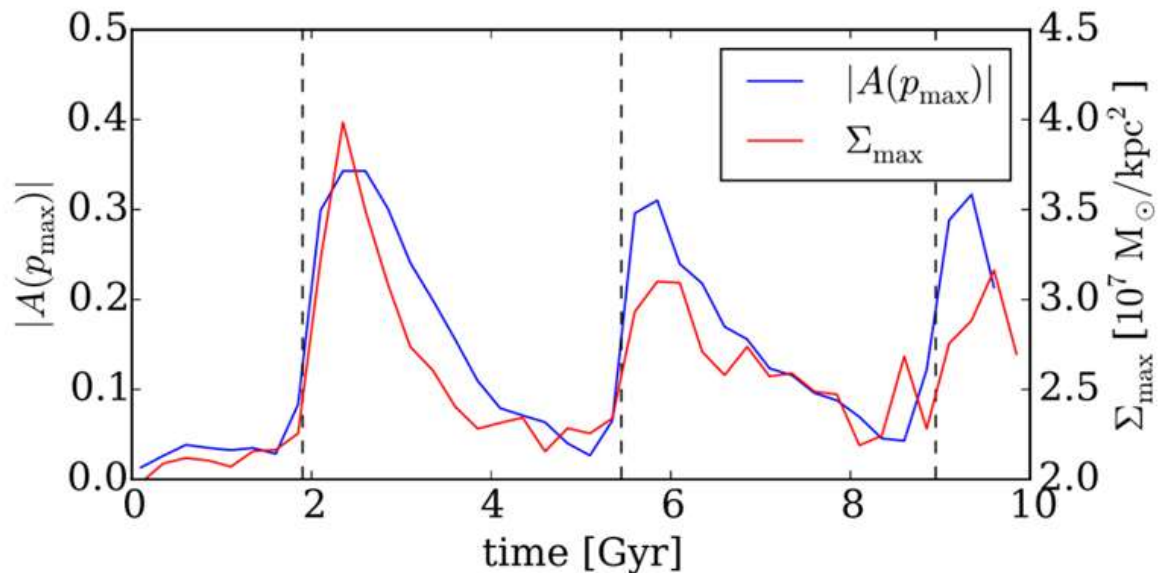
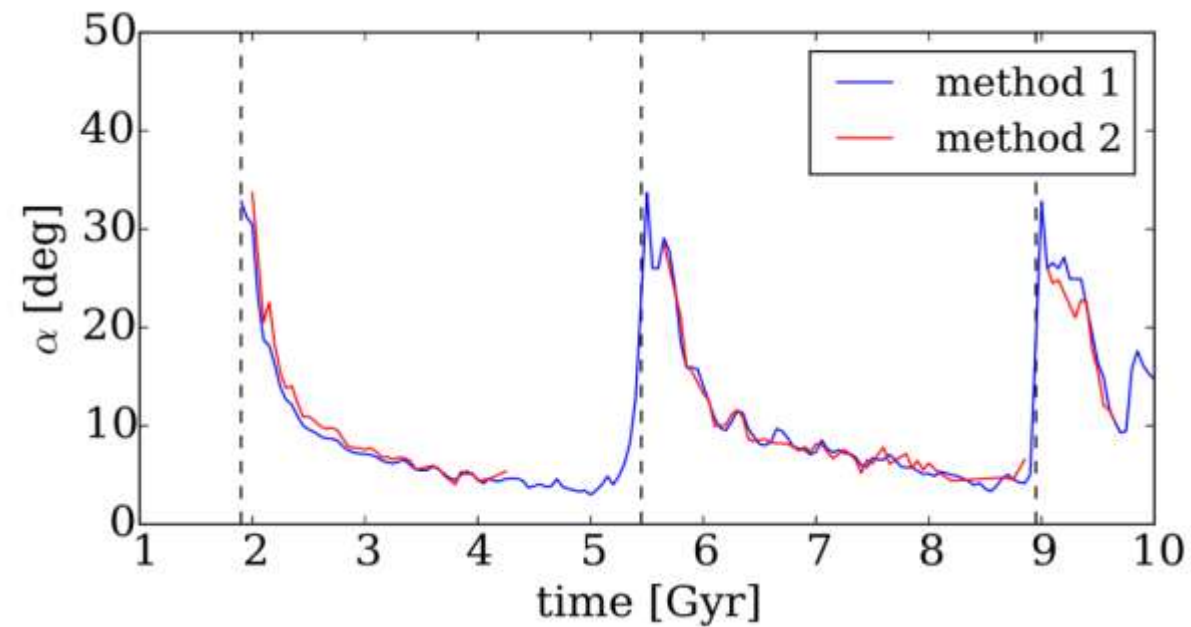
- ☒ Only grand design
- ☒ Spirals without any satellites → DM Halo?

M81

<https://people.astro.umass.edu/~myun/movie.gif>

5. Tidal-Driven Spirals

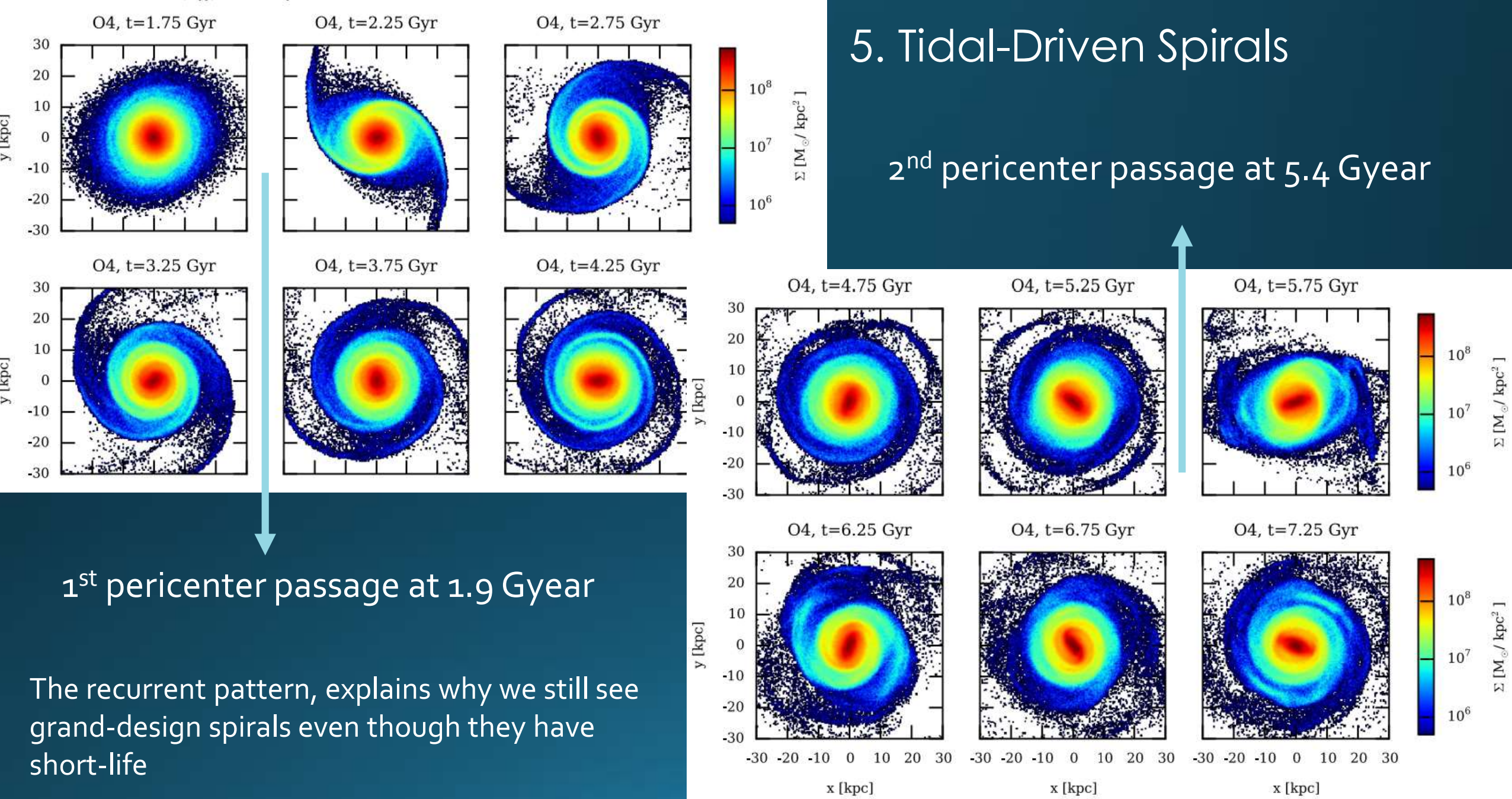
- Strongest arm formation after passage
- 0.5 Gyear of difference between the maximums



$A(p_{\max})$: Strength of the arms
 $\Sigma_{\max}$: Max. surface density distribution of the stars at certain radius

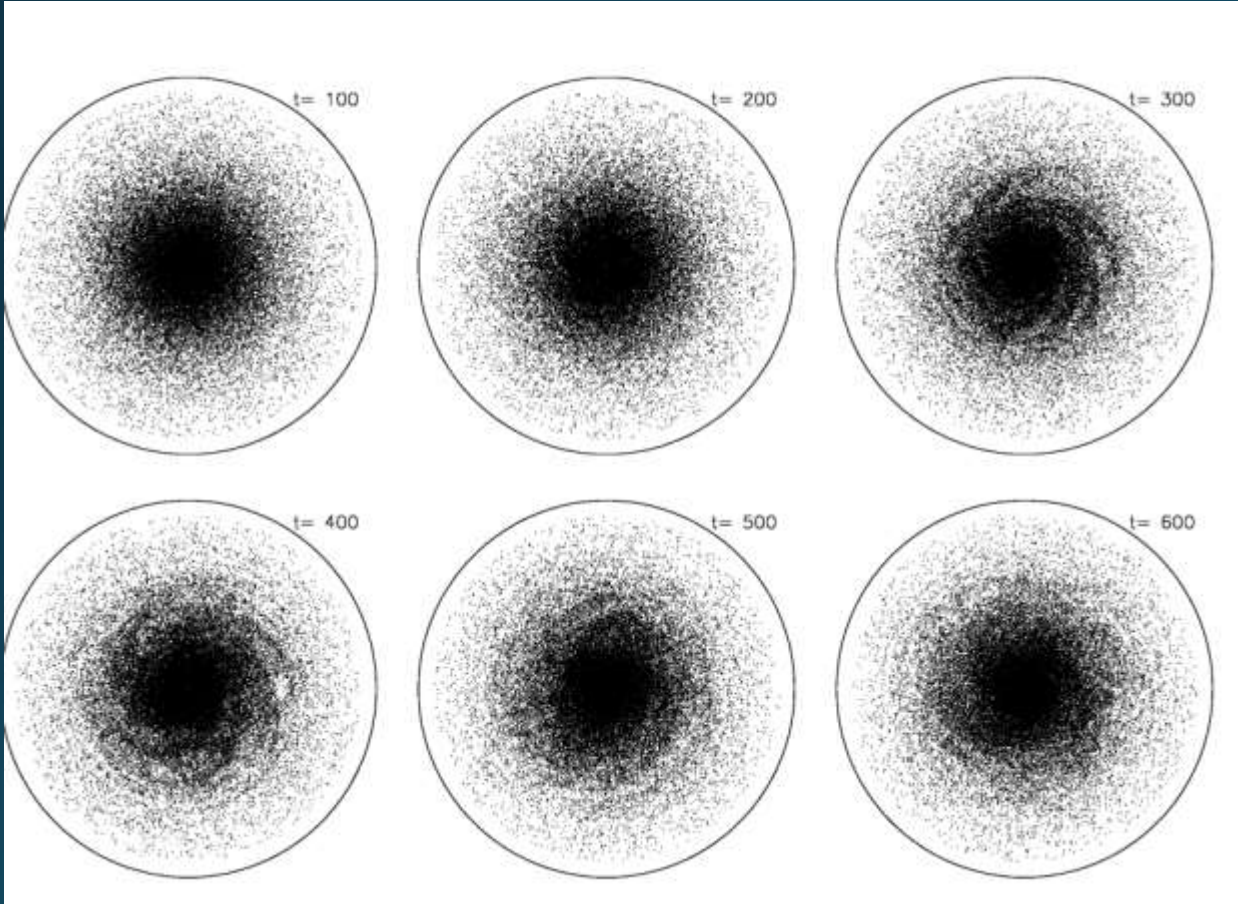
5. Tidal-Driven Spirals

2nd pericenter passage at 5.4 Gyear



6. Lifetime of Spirals

- Simulations by Sellwood (2011):
 - For $m=2$: stable disc over 40 disc rotations
 - For $m \geq 2$: multi-arm short-lived spiral patterns



$$X = \frac{k_{crit} R}{m}$$

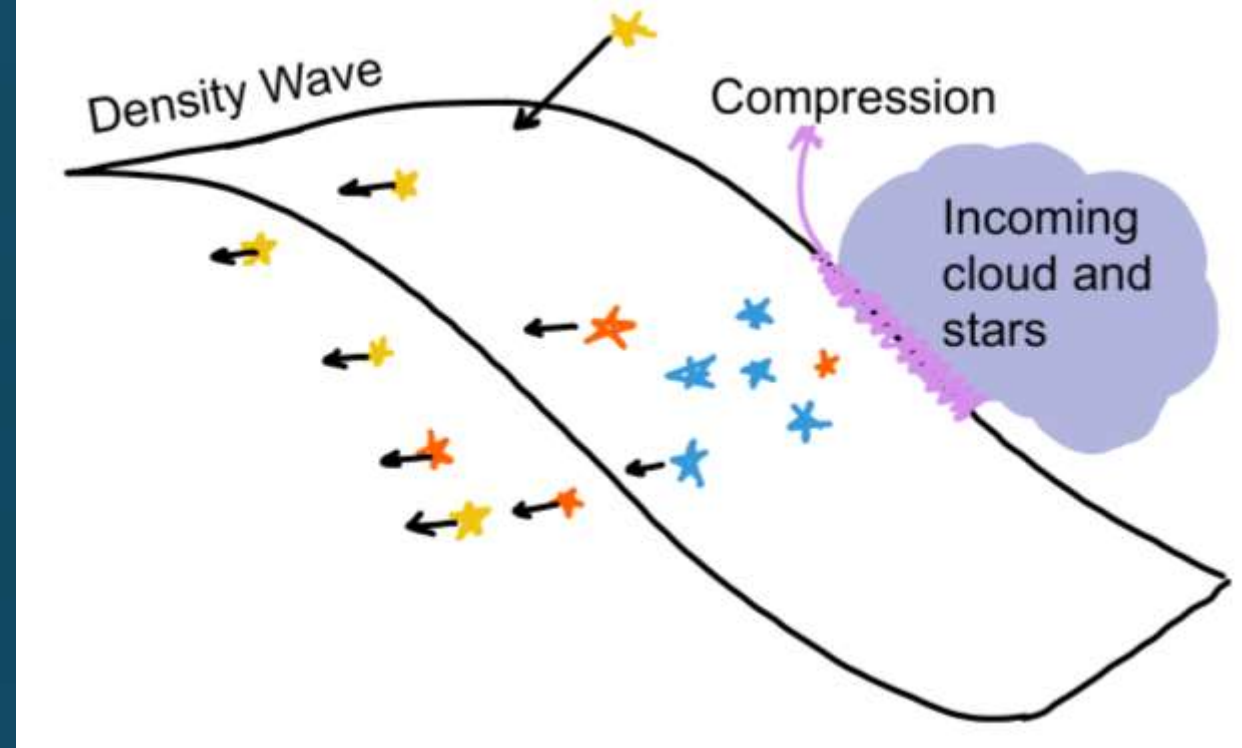
- For $m \geq 4 \rightarrow 1 < X < 2.5 \rightarrow$ vigorous swing amplification
- For $m = 2 \rightarrow$ swing amplification is not effective

6. Lifetime of Spirals

- Angular momentum from inner to outer parts → scattering stars and mixing materials

Transient spirals:

- Scatter disc stars
 - Random motion $\uparrow \rightarrow$ heat up $\rightarrow Q \uparrow$
 - No cooling $\rightarrow$ spirals will disappear
 - cooling $\rightarrow$ fresh stars on circular orbits
 - Lenticular (S0) galaxies: no gas $\rightarrow$ no spirals
-
- Radial Mixing: different metallicities for the same age
 - Stars moving in and out in their radii



NGC 2787

https://en.wikipedia.org/wiki/Lenticular_galaxy



6. Summary

Swing Amplification

- Driven by differential rotation and self-gravity of the disk
- Turning short leading waves to short trailing waves as they pass the CR and amplifying them in the process
- Transient nature and continuous generation

Tidal Interactions:

- A satellite or a DM subhalo (possibly)
- Only grand-design spirals
- Transient spiral due to multiple passages

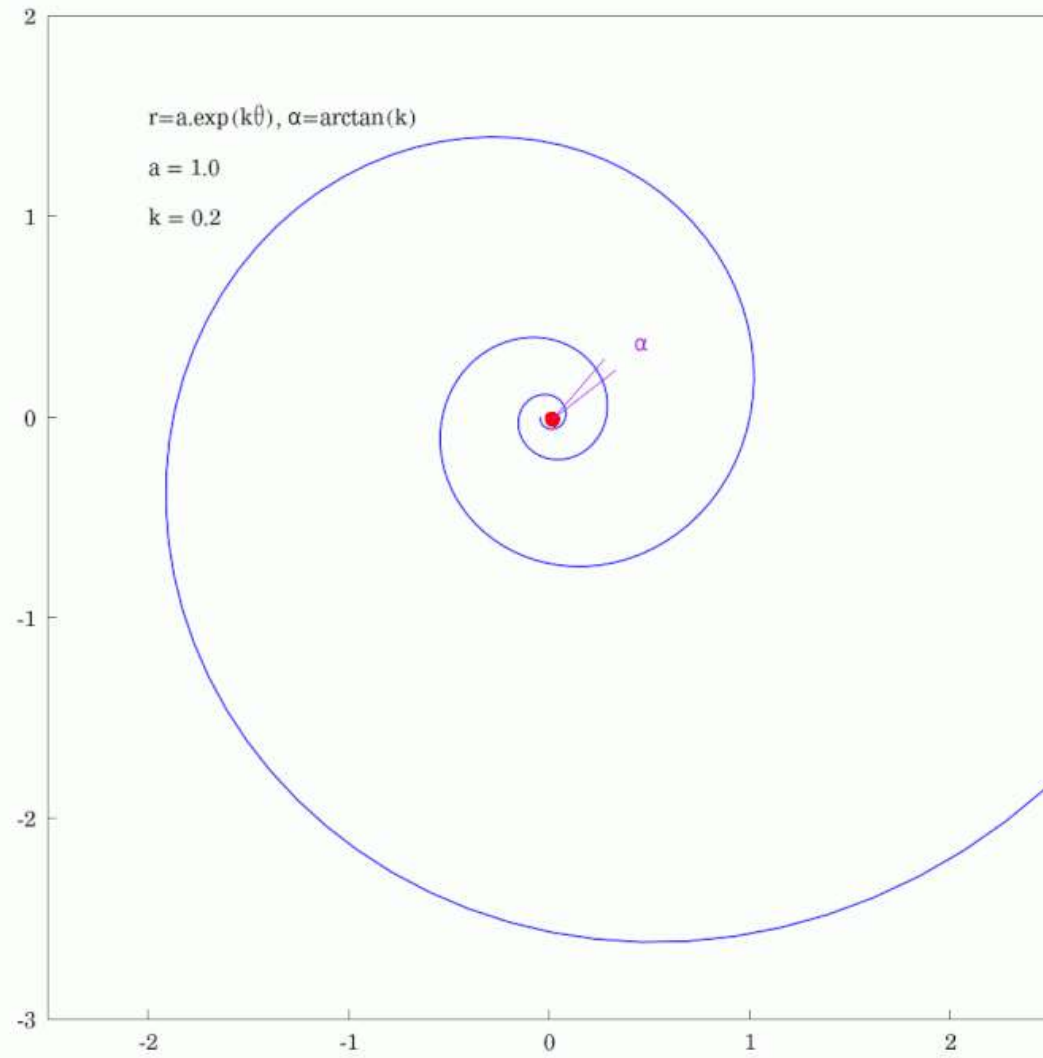
Bar interactions:

- Bar like perturbations
- Long-lived
- Only grand-design
- Common pattern speed

- Simulations and observations point mostly to the transient nature of spiral patterns

Thank you for your attention

Imagining how making the pitch angle smaller will make it more tight/ logarithmics spirals



When does the tidal effect happen

$$S = \left(\frac{M_{\text{pt}}}{M_{\text{gal}}} \right) \left(\frac{R_{\text{gal}}}{d} \right) \left(\frac{\Delta T}{T} \right)^3 \quad (27)$$

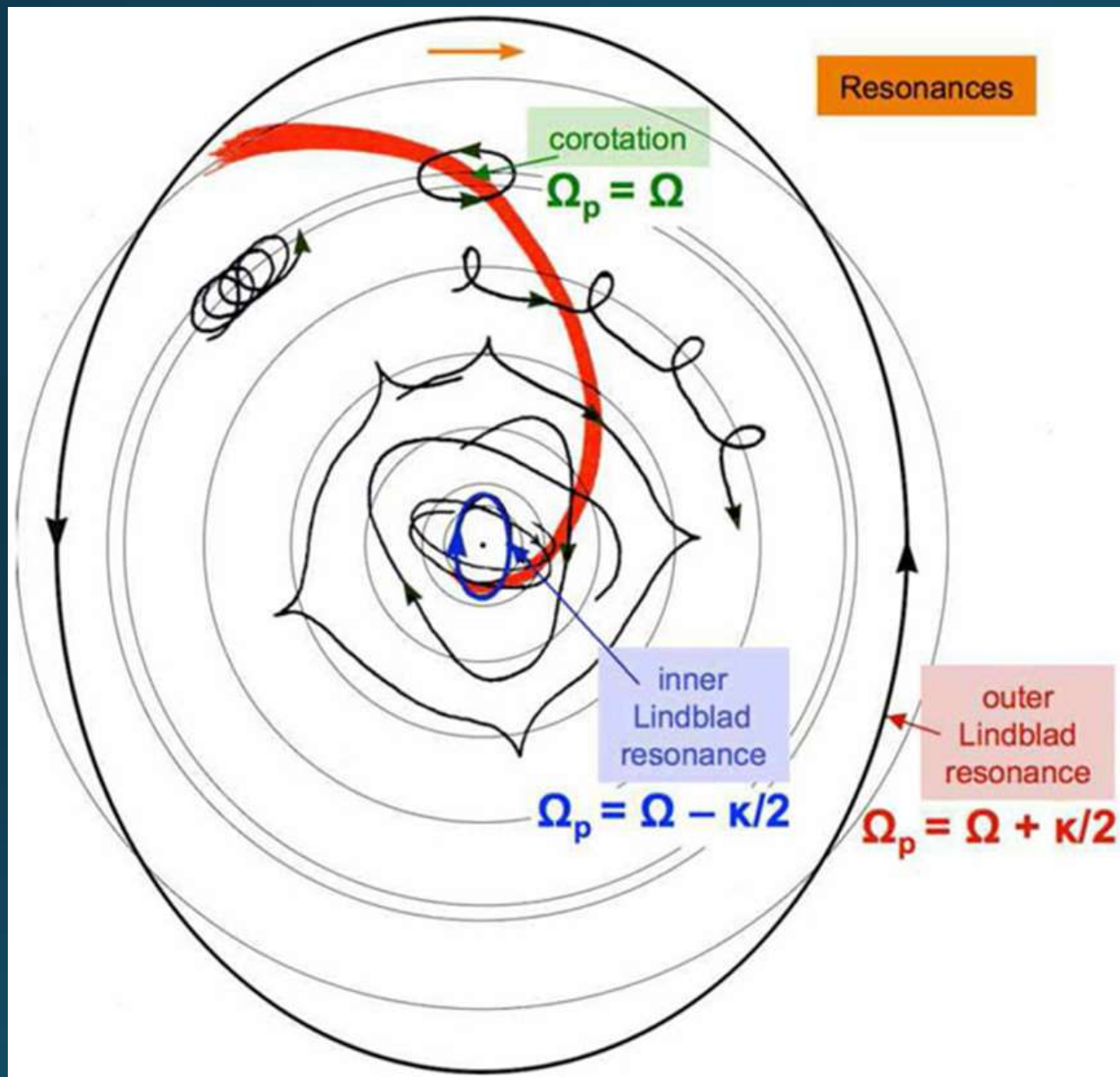
where M_{gal} and R_{gal} are the mass and characteristic size of the perturbed galaxy, M_{pt} is mass of the perturber, d is the closest approach distance between the bodies, ΔT is the interaction time for the perturber to move one radian around the galaxy, and T is the time for stars in the galaxy's outer disk to complete one radian, expressed as $T = (R_{\text{gal}}^3 / GM_{\text{gal}})^{1/2}$. Semczuk et al. (2017) indicated that spiral arms in galaxies can be triggered by smaller companions when S ranges between 0.01 and 0.25 Semczuk et al. (2017).



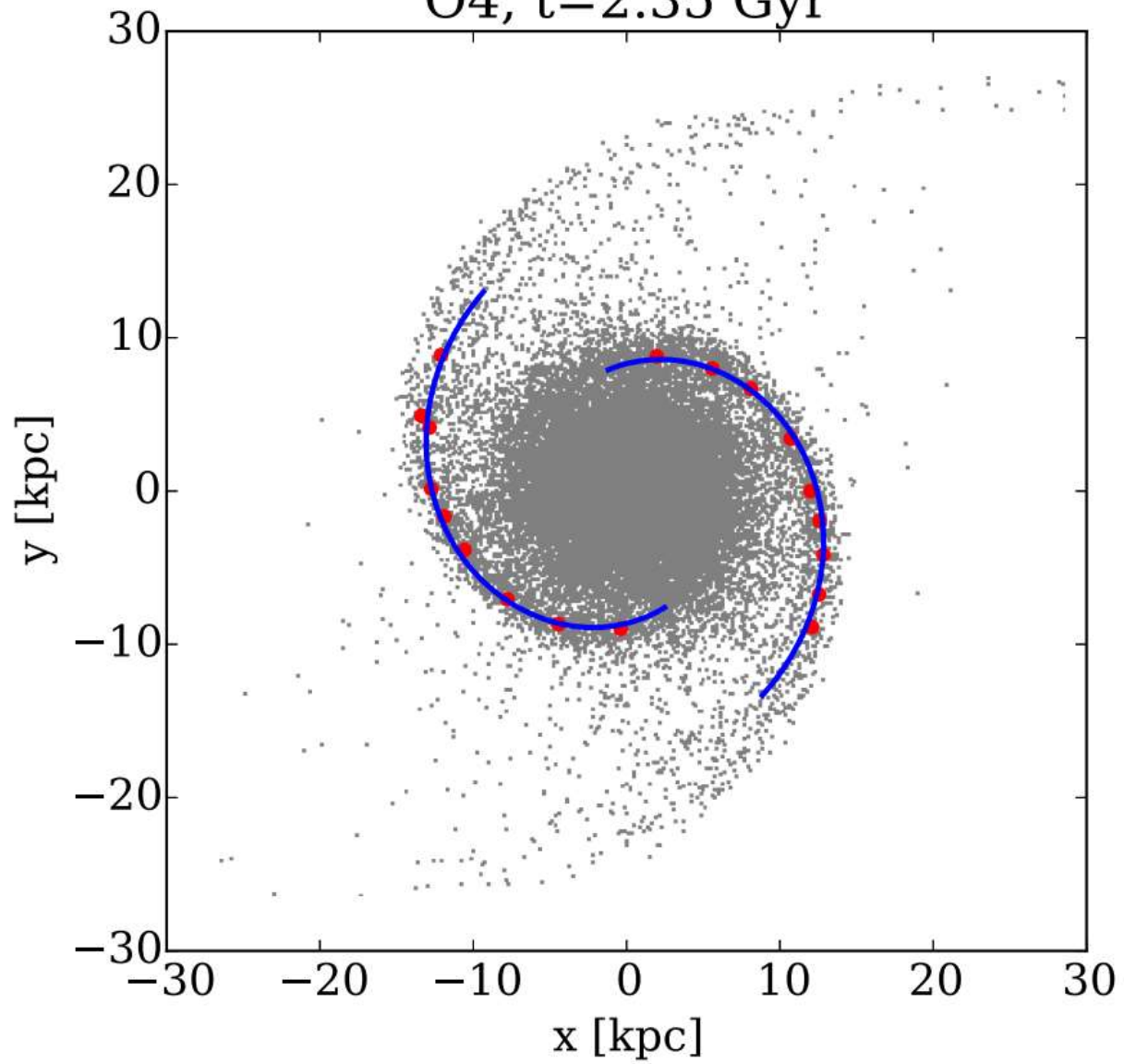
Flocculent



Multi-Armed

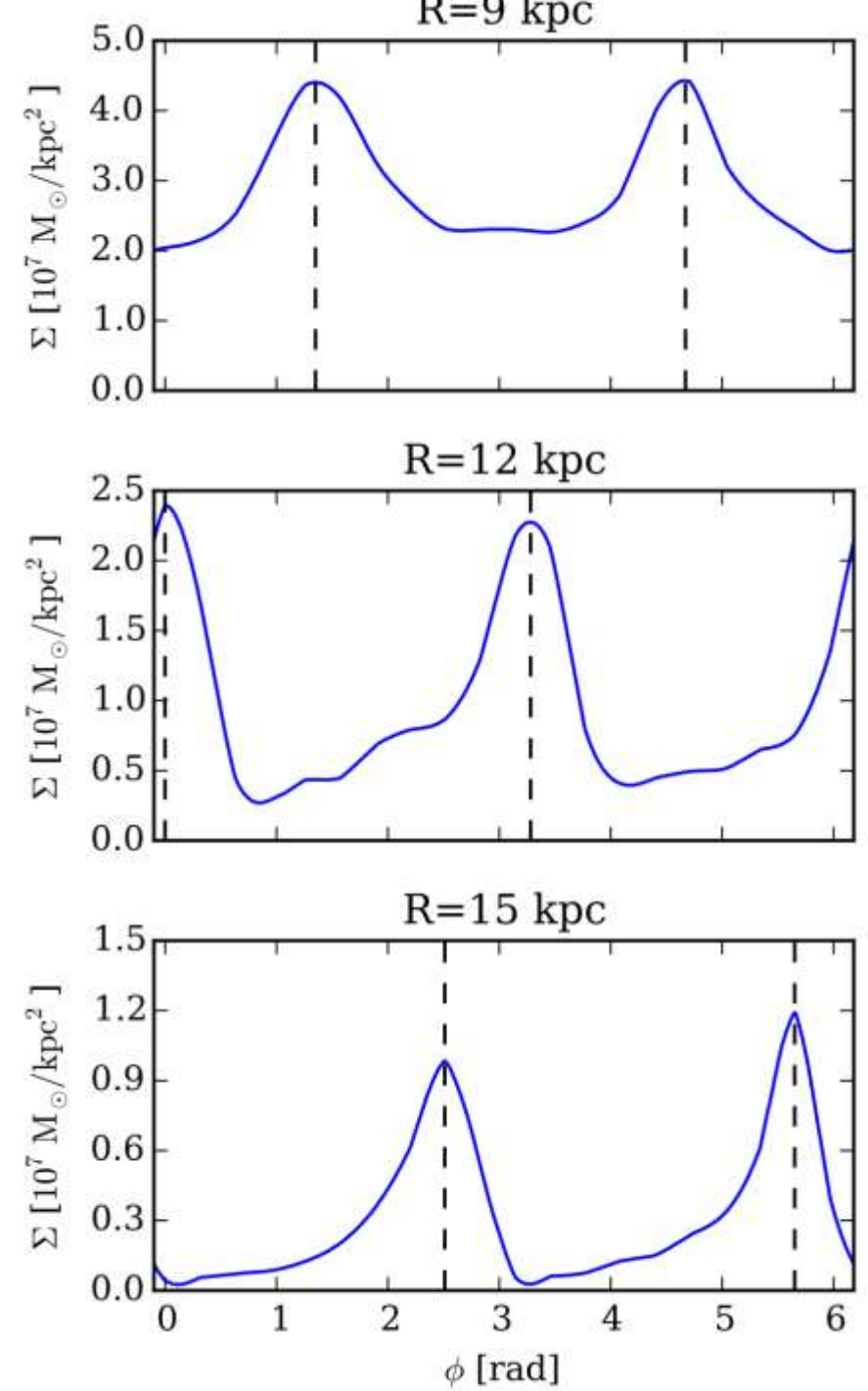


O4, $t=2.35$ Gyr



$$\phi = B \ln R + C$$

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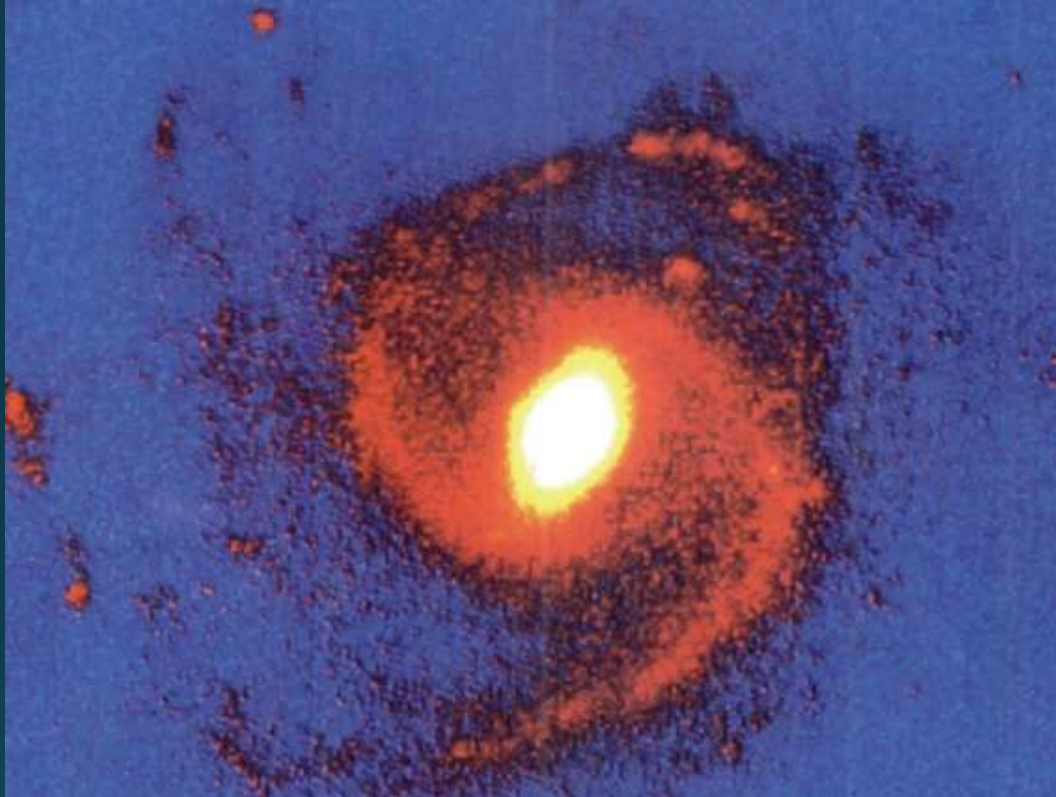
$$A(m, p) = \frac{1}{N_s} \sum_j \exp[i(m\phi_j + p \ln R_j)],$$

$$\tan a = 2/p_{max}$$

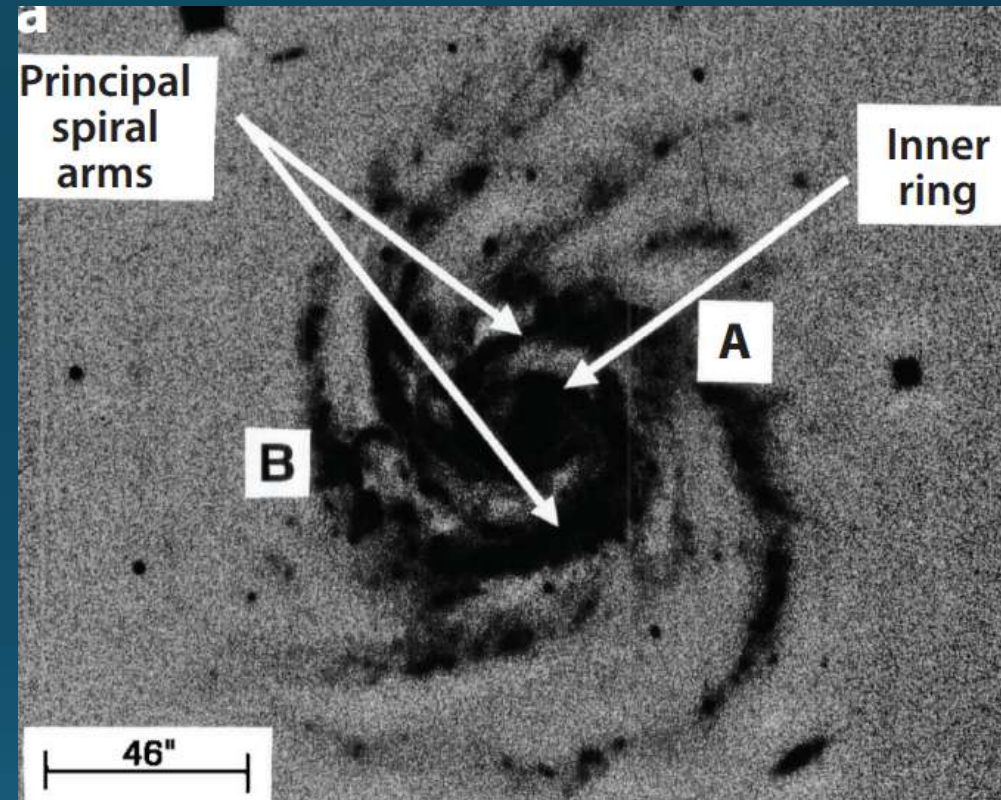
$$F(s, \chi) \equiv \frac{2}{\chi}(1 - s^2)e^{-\chi} \sum_{n=1}^{\infty} \frac{I_n(\chi)}{1 - s^2/n^2},$$

0. Introduction

Shu (2016) Shu, F. H. 2016, ARA&A, 54, 66



NGC 309
Infrared
Grand-Design

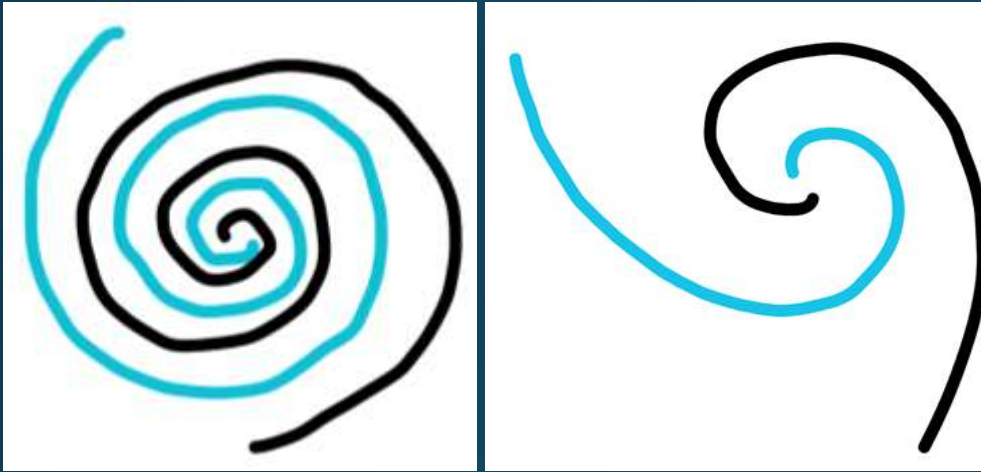


NGC 309
Optical light
Multi-armed almost flocculent

2.1- Dispersion Relation

- Main Hypothesis:

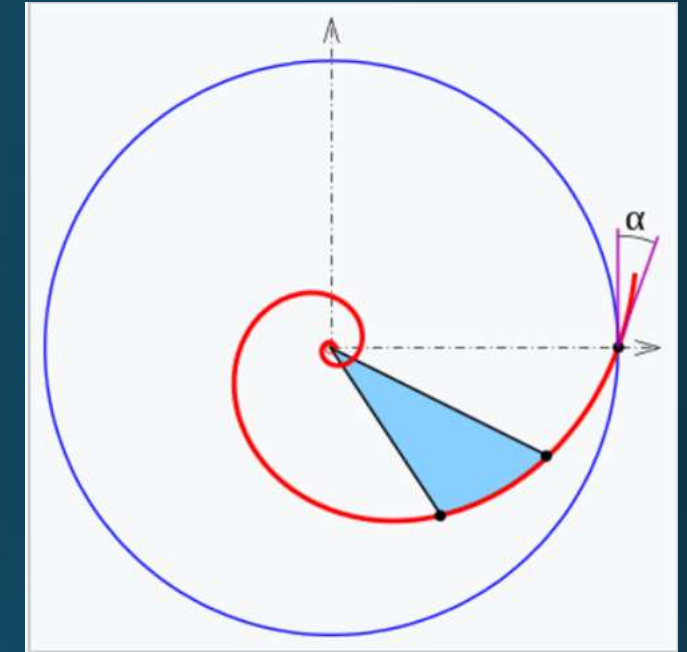
- Tight-Winding Spirals



- Quasi-Stationary Spiral ($\omega = m\Omega_p$)

$$V(r) = \underbrace{V_0(r)}_{\substack{\text{Stationary} \\ \text{Axisymmetric} \\ \text{Bulge, disc, halo}}} + \underbrace{V_1(r)e^{i(\omega t - m\varphi)}}_{\substack{\text{Non-Stationary} \\ \text{Non-Axisymmetric} \\ \text{Spiral Gravitational Perturbation}}}$$

$\gg$



https://en.wikipedia.org/wiki/Pitch_angle_of_a_spiral